

** This examination is open book, but is to be worked on *independently*. You may not discuss or otherwise communicate *any* aspect of the exam with *anyone* other than C. Martin. This includes any discussions with anyone after you are done with the exam, but before the exam's due date and time. This is *very important*.

Due in class, 9:30am, Thursday, May 1

Show your work for full credit. Be concise, but complete.

Avoid long rambling answers which indicate that you don't really understand the question.

1. (30 points) Consider a protein with the following thermodynamic parameters:

$$\Delta H_{298} = -57 \text{ kcal mol}^{-1}$$

$$\Delta S_{298} = -187 \text{ cal mol}^{-1} \text{ K}^{-1}$$

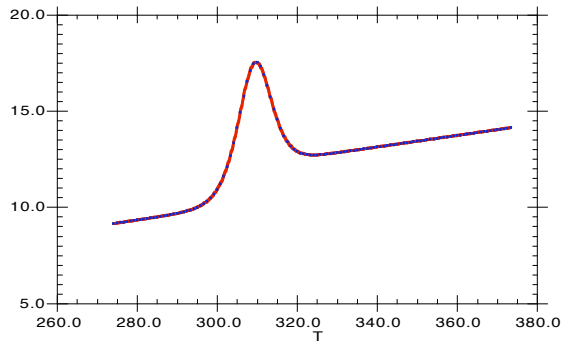
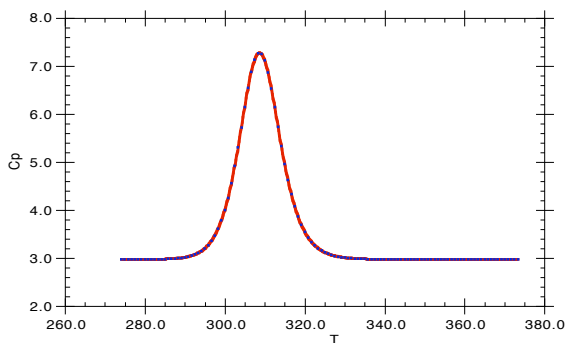
$$\Delta C_p = -2.7 \text{ kcal mol}^{-1}$$

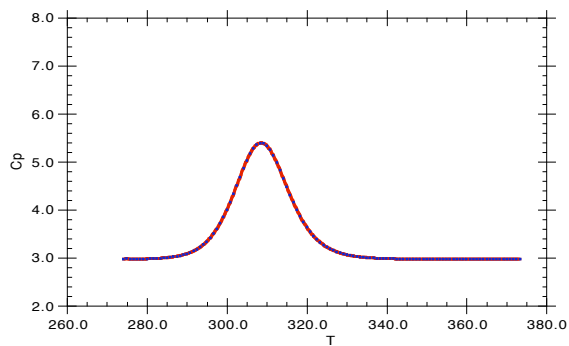
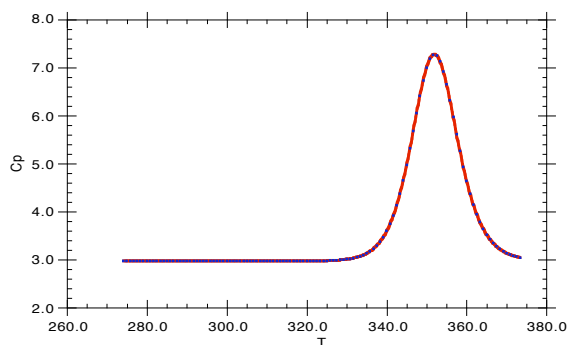
You introduce a small mutation that weakens the enthalpic stability of the protein by only $1.0 \text{ kcal mol}^{-1}$ (less than 2%) at 298K, but has no effect on ΔS_{298} or on ΔC_p). Calculate the effect of this mutation on the stability of the protein, *specifically*, what are the changes in ΔG at 25°C and on the midpoint of the temperature unfolding curve (T_m)?

You may want to “solve” the T_m part graphically (or not)... Note that T_m is the temperature at which you have equal parts folded and unfolded in solution.

ΔG_{298} (native) =	kcal/mol	T_m (native) =	°C
ΔG_{298} (mutant) =	kcal/mol	T_m (mutant) =	°C

2. (40 points) In the following progression of simulated DSC traces of protein thermal denaturation, parameters (from C_p^D , C_p^N , ΔH^o , ΔS^o) were changed from one spectrum to the next. Discuss what you know qualitatively about each of the parameters below. In particular, compare parameters from the various traces – how is one parameter different in one DSC trace from that same parameter in the preceding trace? Bigger, smaller, zero, positive, negative, etc?

 C_p^D C_p^N ΔH^o ΔS^o  C_p^D C_p^N ΔH^o ΔS^o

 C_p^D C_p^N ΔH^o ΔS^o  C_p^D C_p^N ΔH^o ΔS^o

3. (30 points) The following equation shows the temperature dependency of ΔG for a reaction, assuming zero change in heat capacity.

$$\Delta G(T) = \Delta H - T\Delta S$$

We derived in class the following:

$$\Delta G_{T_2} = \Delta H_{T_2} - T_2\Delta S_{T_2}$$

$$\Delta G_{T_2} = \left[\Delta H_{T_1} + \Delta C_p (T_2 - T_1) \right] - T_2 \Delta S_{T_1} + \Delta C_p \ln \frac{T_2}{T_1}$$

$$\Delta G_{T_2} = \Delta H_{T_1} - T_2\Delta S_{T_1} + \Delta C_p (T_2 - T_1) - T_2\Delta C_p \ln \frac{T_2}{T_1}$$

- a) (10 points) Another way of thinking about the temperature dependence of ΔG is to calculate $\Delta\Delta G = \Delta G_{T_2} - \Delta G_{T_1}$. Use the above to derive $\Delta\Delta G$ in terms of ΔG_{T_1} , ΔC_p and ΔS_{T_1} , T_1 and T_2 .

- b) (10 points) The current version of the online lecture notes reflect thinking of the past decade that melting of duplex DNA has a “near-zero” change in heat capacity and therefore ΔH and ΔS can be considered to be independent of temperature. More recently, Bloomfield et al, presented arguments to the contrary. Specifically, for a particular oligonucleotide at its melting temperature (72°C), the following parameters were determined:

$$\Delta C_p = 65.3 \frac{\text{cal}}{\text{mol K}} \quad \Delta S = 24.9 \frac{\text{cal}}{\text{mol K}}$$

Use the equation you derived in (b) to argue that this value of ΔC_p is “not negligible.” How far off is it?

- c) (10 points) Use the equation from part (b) to calculate the value for ΔH at 72°C.