## Energy of a System

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We can also do WORK on a system, as a way of putting energy into the system
Or the system can do work, which takes energy out of the system

Change in energy content

## Energy transferred as

 work to or from the system

$$
\Delta U=q+w
$$

Positive value: energy INTO the system

## Energy transferred as heat to or from the system

Work (at constant pressure)


$$
w=-P \times \Delta V
$$



Pressure



$$
\begin{aligned}
& w=-P\left(V_{\text {final }}-V_{\text {initial }}\right) \\
& w=-(1 \mathrm{~atm})(0.1 \mathrm{~L}-0.5 \mathrm{~L})=+0.4 \mathrm{~atm} \cdot L
\end{aligned}
$$



$$
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Work is positive.
Work is done ON system Energy of system increases


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From inside back of book

$$
R=8.3144 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}} \quad R=0.082057 \frac{\mathrm{~L} \cdot \mathrm{~atm}}{\mathrm{~K} \cdot \mathrm{~mol}}
$$



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& \mathrm{~L} \cdot \mathrm{~atm}=101.32 \mathrm{~J}
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& L \cdot \mathrm{~atm}=101.32 \mathrm{~J} \\
& w=+0.4 \mathrm{~atm} \cdot L\left(\frac{101.32 \mathrm{~J}}{\mathrm{~atm} \cdot L}\right)=40.53 \mathrm{~J}
\end{aligned}
$$

A Closer Look, p. 225
q and w

## q and w

## Energy transferred as heat to system (endothermic)

## q and w

## Energy transferred as heat to system (endothermic) <br> $q>0$

Energy transferred as heat from system (exothermic) q<0

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Energy transferred as work done on system

## q and w

Energy transferred as heat to system (endothermic) $\quad \mathrm{q}>0$

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Energy transferred as work done on system
$w>0$

Energy transferred as word done by system
w<0

## q and w

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Energy transferred as work done on system
$w>0$

Energy transferred as word done by system
$w<0$

## q and w

Energy transferred as heat to system (endothermic) $\quad q>0 \quad U \uparrow$

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Energy transferred as heat to system (endothermic) $\quad q>0 \quad U \uparrow$

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Energy transferred as work done on system
Us 0

Energy transferred as word done by system
$w<0$

## q and w

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## $\Delta \mathrm{H}$ - enthalpy

Assume reaction at constant pressure

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$$
\begin{aligned}
\Delta U & =q_{p}+w_{p} \\
\Delta U & =q_{p}-P \Delta V \\
\therefore \quad q_{p} & =\Delta U+P \Delta V
\end{aligned}
$$

$$
\begin{aligned}
& \text { Define }: H=U+P V \\
& \therefore \Delta H=\Delta U+P \Delta V \\
& \therefore \Delta H=q_{p}
\end{aligned}
$$

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Bottom line:
almost all of biology occurs at 1 atm pressure (constant)

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Bottom line:
almost all of biology occurs at 1 atm pressure (constant)
$\Delta \mathrm{H}$ is a useful measure of the change in energy of a system

$$
\begin{aligned}
& \text { Define }: H=U+P V \\
& \therefore \Delta H=\Delta U+P \Delta V \\
& \therefore \Delta H=q_{p}
\end{aligned}
$$



## Energy is a State Function

## A state function defines a system

 independent of "how you got there"State Functions:
Energy $(\Delta \mathrm{U}, \Delta \mathrm{H})$
Pressure
Volume
Temperature
Elevation
Your bank balance

NOT State Functions:
Driving distance to Boston
q
W

## Enthalpy $(\Delta \mathrm{H})$ of a reaction

$\mathrm{H}_{2} \mathrm{O}(\mathrm{g}) \longrightarrow \mathrm{H}_{2}(\mathrm{~g})+1 / 2 \mathrm{O}_{2}(\mathrm{~g}) \quad \Delta \mathrm{H}^{\circ}=+241.8 \mathrm{~kJ} /$ mole-rxn
What does this tell us?
$\Delta H>0$ endothermic.
Have to put energy in (heat) to make the reaction go to the right as written
241.8 per mole as written (per $1 \mathrm{H}_{2} 0$ consumed, or per $1 \mathrm{H}_{2}$ produced)

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What is $\Delta \mathrm{H}^{\circ}$ for

$$
2 \mathrm{H}_{2} \mathrm{O}(\mathrm{~g}) \longrightarrow 2 \mathrm{H}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g})
$$

## Enthalpy $(\Delta \mathrm{H})$ of a reaction

$\mathrm{H}_{2} \mathrm{O}(\mathrm{g}) \longrightarrow \mathrm{H}_{2}(\mathrm{~g})+1 / 2 \mathrm{O}_{2}(\mathrm{~g})$
What is $\Delta H^{\circ}$ for
$2 \mathrm{H}_{2} \mathrm{O}(\mathrm{g}) \longrightarrow 2 \mathrm{H}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g})$

## Enthalpy $(\Delta \mathrm{H})$ of a reaction

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$$
\begin{array}{cr}
\mathrm{H}_{2} \mathrm{O}(\mathrm{~g}) \longrightarrow \mathrm{H}_{2}(\mathrm{~g})+1 / 2 \mathrm{O}_{2}(\mathrm{~g}) & \Delta \mathrm{H}^{\circ}=+241.8 \mathrm{~kJ} / \mathrm{mole}-\mathrm{rxn} \\
\stackrel{\mathrm{H}_{2} \mathrm{O}(\mathrm{~g}) \longrightarrow \mathrm{H}_{2}(\mathrm{~g})+1 / 2 \mathrm{O}_{2}(\mathrm{~g})}{2 \mathrm{H}_{2} \mathrm{O}(\mathrm{~g}) \longrightarrow 2 \mathrm{H}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g})} & \Delta \mathrm{H}^{\circ}=+241.8 \mathrm{~kJ} / \mathrm{mole}-\mathrm{rxn} \\
\hline \mathrm{H}^{\circ}=+2(241.8 \mathrm{~kJ} / \mathrm{mole}-\mathrm{rxn})
\end{array}
$$

$\Delta \mathrm{H}^{\circ}=+483.6 \mathrm{~kJ} / \mathrm{mole}-\mathrm{rxn}$

## Chemical Equation Accounting/Math

$\mathrm{C}(\mathrm{s})+\mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{CO}(\mathrm{g})+1 / 2 \mathrm{O}_{2}(\mathrm{~g}) \quad \Delta \mathrm{H}^{\circ}=-110.5 \mathrm{~kJ} / \mathrm{mol}$
$\mathrm{CO}(\mathrm{g})+1 / 2 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{CO}_{2}(\mathrm{~g})$
$\Delta H^{\circ}=-283.0 \mathrm{~kJ} / \mathrm{mol}$
$\mathrm{C}(\mathrm{s})+\mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{CO}_{2}(\mathrm{~g})$
$\Delta \mathrm{H}^{\circ}=? ? \mathrm{~kJ} / \mathrm{mol}$

Chemical Equation Accounting/Math
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$\mathrm{C}(\mathrm{s})+\mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{CO}_{2}(\mathrm{~g})$
$\Delta H^{\circ}=-393.5 \mathrm{~kJ} / \mathrm{mol}$

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$$
\mathrm{C}(\mathrm{~s})+\mathrm{O}_{2}(\mathrm{~g})
$$

$$
\underbrace{-110.5 \mathrm{~kJ}} \begin{gathered}
\Delta_{\mathrm{r}} H_{1}^{\circ}= \\
-110(\mathrm{~g})+\frac{1}{2} \mathrm{O}_{2}(\mathrm{~g})
\end{gathered}
$$

$$
\begin{aligned}
& \mathrm{C}(\mathrm{~s})+\mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{CO}(\mathrm{~g})+1 / 2 \mathrm{O}_{2}(\mathrm{~g}) \\
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& \mathrm{C}(\mathrm{~s})+\mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{CO}_{2}(\mathrm{~g})
\end{aligned}
$$

## Energy

$$
\begin{gathered}
\Delta_{\mathrm{r}} H_{3}^{\circ}= \\
\Delta_{\mathrm{r}} H_{1}^{\circ}+\Delta_{\mathrm{r}} H_{2}^{\circ} \\
=-393.5 \mathrm{~kJ}
\end{gathered}
$$

$$
\begin{gathered}
\Delta_{\mathrm{r}} H_{2}^{\circ}= \\
-283.0 \mathrm{~kJ}
\end{gathered}
$$

$$
\begin{aligned}
& \Delta H^{\circ}=-110.5 \mathrm{~kJ} / \mathrm{mol} \\
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$\Delta H^{\circ}=-393.5 \mathrm{~kJ} / \mathrm{mol}$
$\mathrm{CO}_{2}(\mathrm{~g})$
(a) The formation of $\mathrm{CO}_{2}$ can occur in a single step or in a succession of steps. $\Delta_{\mathrm{r}} H^{\circ}$ for the overall process is -393.5 kJ , no matter which path is followed.

$$
\mathrm{C}(\mathrm{~s})+\mathrm{O}_{2}(\mathrm{~g})
$$

$$
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$$
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$$
\Delta H^{\circ}=-393.5 \mathrm{~kJ} / \mathrm{mol}
$$

$$
\mathrm{CO}_{2}(\mathrm{~g})
$$

(a) The formation of $\mathrm{CO}_{2}$ can occur in a single step or in a succession of steps. $\Delta_{\mathrm{r}} H^{\circ}$ for the overall process is -393.5 kJ , no matter which path is followed.

(b) The formation of $\mathrm{H}_{2} \mathrm{O}(\ell)$ can occur in a single step or in a succession of steps. $\Delta_{\mathrm{r}} H^{\circ}$ for the overall process is -285.8 kJ , no matter which path is followed.


## Phase Change!

(b) The formation of $\mathrm{H}_{2} \mathrm{O}(\ell)$ can occur in a single step or in a succession of steps. $\Delta_{\mathrm{r}} H^{\circ}$ for the overall process is -285.8 kJ , no matter which path is followed.

Energy level diagram for the decomposition of $\mathrm{CaCO}_{3}(\mathrm{~s})$


## Math Gymnastics: What's it Good For?

$\Delta H_{f}^{\circ}$

## Math Gymnastics: What's it Good For?

## Standard enthalpies of formation

Appendix L - page A29

$\Delta H_{f}^{\circ}$

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 Appendix L - page A29$\Delta H_{f}^{\circ}$

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Standard enthalpies of formation Appendix L - page A29



1-butene


## TABLE 2 Energy Released by Combustion of Fossil Fuels

Substance

Energy Released (kJ/g)

| Coal | $29-37$ |
| :--- | :---: |
| Crude petroleum | 43 |
| Gasoline (refined petroleum) | 47 |
| Natural gas (methane) | 50 |

TABLE 1 Producing Electricity in theUnited States (2006)
Coal ..... 50\%
Nuclear ..... 19\%
Natural gas ..... 19\%
Hydroelectric ..... 7\%
Petroleum ..... 3\%
Other renewables ..... 2\%

## TABLE 3 Types of Coal

| Type | Consistency | Sulfur Content | $(\mathrm{kJ} / \mathrm{g})$ |
| :--- | :--- | :--- | :--- |
| Lignite | Very soft | Very low | $28-30$ |
| Bituminous coal | Soft | High | $29-37$ |
| Anthracite | Hard | Low | $36-37$ |


(a) Methane hydrate burns as methane gas escapes from the solid hydrate.
(b) Methane hydrate consists of a lattice of water molecules with methane molecules trapped in the cavity.



$\mathrm{H}_{2}$ gas
8
Metaladsorbed hydrogen


Solid solution $\alpha$-phase

Hydride phase $\beta$-phase $\infty$
 $\beta$-phase

Metal hydride
Electrolyte


## Isooctane <br> $\mathrm{C}_{8} \mathrm{H}_{18}$

