

10/29/01 Ave = 73 ± 17 Median = 77
(39-99)

(41)

Note $k = \frac{R}{N_0}$ $k \Rightarrow$ per molecule

$R \Rightarrow$ per mole

Whenever you see k ,
it's per molecule

Whenever you see R ,
it's per mole

BIG PICTURE \rightarrow every molecule has an average
kinetic energy of $\frac{3}{2}kT$

DISTRIBUTIONS about the average

MAXWELL-BOLTZMANN

BOLTZMANN \rightarrow

Probability of finding a
molecule in state i w/ energy E_i

$$P_i \propto e^{-E_i/kT}$$

If there are g_i states w/ energy E_i
then

Probability of
finding a molecule
w/ energy E_i

$$P_i \propto g_i e^{-E_i/kT}$$

\uparrow
degeneracy

N.B.

**IMPORTANT
EQUATION!**

P_i is relative to all other P_j 's

$\frac{-\Delta_d RT}{e}$
per mole

$$P_j = \frac{g_j e^{-E_j/KT}}{\sum_i g_i e^{-E_i/KT}} = \frac{N_j}{N_{TOT}}$$

SAVE
we'll use
often

(Remember $\sum_{ALL} P_i = 1$)

SKIP SOME DERIVATIONS

Also

mean speed
(not velocity) $\langle u \rangle = \left(\frac{8KT}{\pi m} \right)^{1/2}$

$$\frac{N_j}{N} = \frac{g_j}{g_i} e^{-(E_j - E_i)/KT}$$

mean square speed
(or velocity) $\langle u^2 \rangle = \frac{3KT}{m}$

Molecular Collisions - First step to a reaction.

Root mean square speed = $\sqrt{\langle u^2 \rangle} = \sqrt{\frac{3KT}{m}} = 218 \text{ m s}^{-1}$
rose scout at R.T.

Intuition says "wait a minute!"

Collisions slow the NET diffusion

Diff. Walk across an empty room
Walk across a crowded room, drunk(!)
(random)

Collisions per sec = z for 1 molecule

Q: Proportional to what?

A: Conc ($\frac{N}{V}$)
Speed (u)
Size (σ)



Real answer:

$$z \propto \frac{N}{V} \sigma^2 \langle u \rangle$$

Actually $z = \sqrt{2} \pi \frac{N}{V} \sigma^2 \langle u \rangle \Rightarrow \left(\frac{\text{molec}}{\text{cm}^3} \right) (\text{cm}^2) \left(\frac{\text{cm}}{\text{sec}} \right)$

Plugging in for $\langle u \rangle$

$$z = 4 \sqrt{\pi} \frac{N}{V} \sigma^2 \left(\frac{RT}{M} \right)^{1/2}$$

Total # Collisions $\frac{N}{V} \Rightarrow \frac{\text{molec}}{\text{Volume}}$

$$\therefore \frac{N}{V} z \Leftarrow \frac{\text{molecules colliding}}{(\text{Volume} \times \text{time})}$$

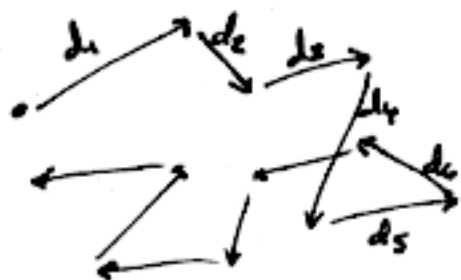
$$\frac{\text{Collisions}}{\text{Vol} \cdot \text{time}} = Z = \left(\frac{N}{V} \right) \frac{z}{2} = 2 \sqrt{\pi} \left(\frac{N}{V} \right)^2 \sigma^2 \left(\frac{RT}{M} \right)^{1/2}$$

~~for self collisions~~ Don't count each collision twice

(4)

Mean Free Path \Rightarrow average distance between collisions

Brownian Motion
Random Walk



$$l = \frac{\langle u \rangle}{z} = \frac{\text{dist/time}}{\text{collisions/time}}$$

$$l = \frac{1}{\sqrt{2} \pi \left(\frac{N}{V}\right) \sigma^2}$$

$$\langle d^2 \rangle = \frac{\sum_{\text{paths}} d_i^2}{\# \text{ paths}}$$

$$= N l^2$$

$$\sqrt{\langle d^2 \rangle} = \sqrt{N} l \quad \Leftrightarrow \text{Applications everywhere.}$$

GAS MOLECULES

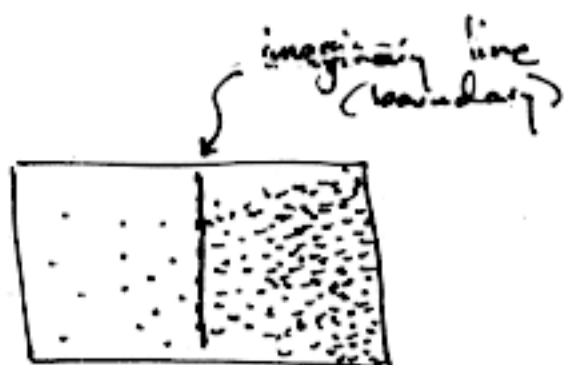
$$(\langle d^2 \rangle)^{1/2} = \sqrt{z} l = \frac{\langle u \rangle}{\sqrt{z}}$$

$$\langle d^2 \rangle = \frac{\langle u^2 \rangle^2}{z}$$

$$(\langle d^2 \rangle)^{1/2} = \frac{\langle u \rangle}{\sqrt{z}}$$

Diffusion

Probability that any molecule crosses from left to right is much lower than that for any molecule moving from right to left



conc →

← Purely intuitional common sense

$J_x \equiv$ net amount of molecules crossing the boundary per unit time.

$$J_x \propto -\frac{dc}{dx} \quad \leftarrow \text{magnitude of the gradient}$$

$$J_x = -D \frac{dc}{dx}$$

But as diffusion occurs, the gradient lessens.
 $\therefore J_x$ slows

$$\left(\frac{dc}{dt}\right)_x = D \left(\frac{d^2c}{dx^2}\right)_x$$

Change in concentration w/ time

\propto

2ND derivative of change in conc w/ resp to x .

(D assumed to be indep of C)