

Chapter 9 - 2, 3, 4, 5, 6, 7, 13, 16, 23a

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Chapter 8 - Suggested Chapter problems

1-7, 9, 10a-d, 12, 13, 14, 16, 18, 19, 21a, 22, 25

Chapter 9 Reading - Skip "Tunneling" pp 463-464

DO Read ~~Skip~~ "Harmonic Osc" pp 465-467

Skip "Rigid Rotator" pp 468-469

DO Read "Hydrogen Atom" and sections following
ie pp. 469-476

Skip "Many Electron Atoms" pp. 476-478

Read lightly 479-490. Skip 491-513

Read 514-~~14~~
517

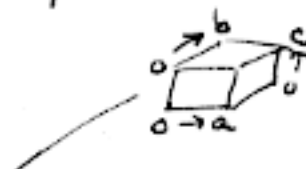
Review past 2 lectures - Chapter 9

Wave-particle duality - small particles show wave-like prop's

Describe wave behavior by wave function: $\psi(x, y, z)$

$\psi^2(x, y, z) \rightarrow \psi^2 \propto$ Probability of finding e^- at x, y, z

Finite Probability = $\int_0^a \int_0^b \int_0^c \psi^2 dz dy dx$



$$\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \psi^2 dx dy dz = 1$$

Operator \Leftrightarrow Expectation Value

$$\bar{z} = \int \psi_n^* z \psi_n d\tau$$

$$E = \int \psi_n^* \mathcal{H} \psi_n d\tau$$

ONE-DIMENSION

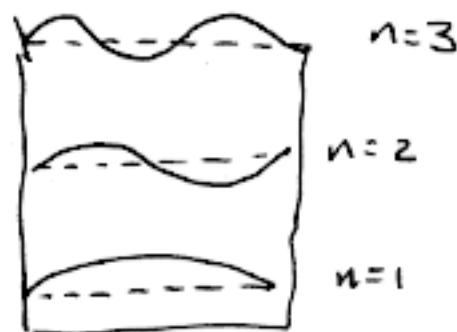
$$\mathcal{H} = \frac{\hbar^2}{2m} \frac{d^2}{dx^2} + U(x)$$

One Dimensional Particle in a Box - A really simple atom

Use $\int_{-\infty}^{\infty} \Psi^2 dx = 1$ and Boundary Conditions to yield

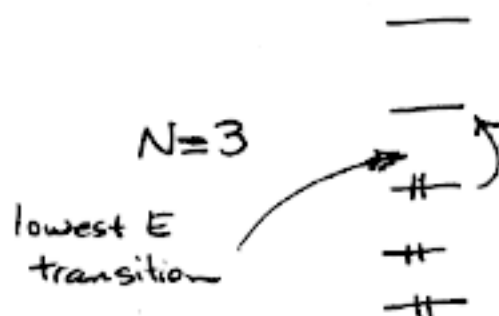
$$\Psi_n = \sqrt{\frac{2}{a}} \sin\left(\frac{n\pi}{a} x\right)$$

$$E_n = \frac{h^2 n^2}{8ma^2}$$



$$\lambda_{N \rightarrow N+1} = \frac{8mca^2}{h(2N+1)}$$

N = Quantum number of the highest filled orbital
(For simple atom, $N = \frac{1}{2} (\# \text{ electrons})$)

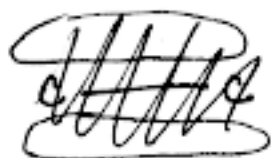
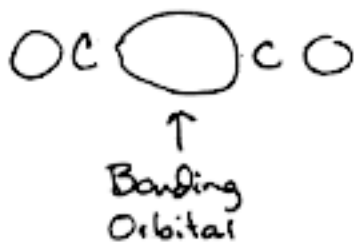


Particle in a Box had a very simple $U(x)$.

Fancier Version

Harmonic Oscillator

Elaborate why



$F = -kx$
 $U = \frac{1}{2} kx^2$
 $C - \text{cosine} - C$

$$\mathcal{H} = \frac{h^2}{2m} \frac{d^2}{dx^2} + \frac{1}{2} kx^2$$

x = deviation from lowest E length

\Rightarrow

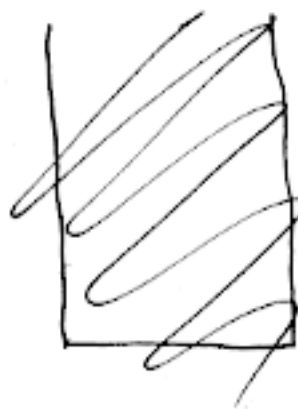
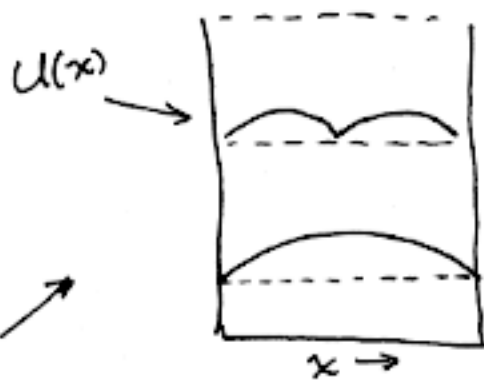
Again, one-dimensional

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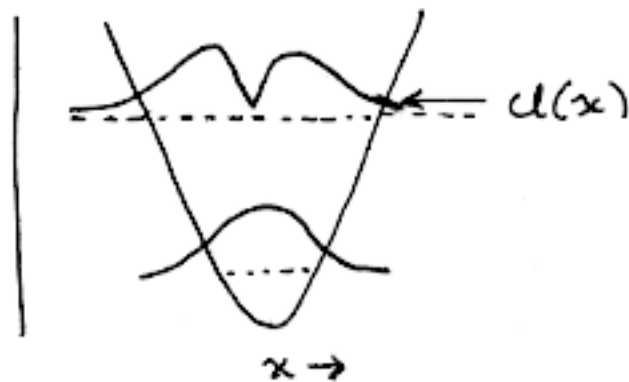


↑ Bonding orbital

$$-\frac{\hbar^2}{2m} \frac{d^2 \psi}{dx^2} + \frac{1}{2} k x^2 \psi = E \psi$$



Note similarities



Good descriptor for BOND wavefunctions

Quantized energy levels $\Rightarrow n = 1, 2, 3, 4, \dots$

see p. 465

Harmonic oscillator is used as a wavefunction

for many molecular dynamics and molecular mechanics calculations. NOT BAD

H Atom - 3 Dimensions / move from x, y, z to polar coords.

$$\mathcal{H} = \frac{\hbar^2}{2m} \frac{d^2}{dx^2} + \frac{-e^2}{4\pi\epsilon_0 r}$$

radius of e⁻ from center (nucleus)

3 QUANTUM NUMBERS - POLAR COORDS

n, l, m
↑ radial angular

Back to General Chemistry
Reduced mass → "m"
→ Related to moment of inertia

TAKE HOME → Quantized values for energy

$$E_n = -\frac{\mu e^4}{2\hbar^2 n^2}$$

n = 1, 2, 3, ...

READ pp 469-476
H-atom

Read lightly pp. 479-490 and relate it back to your General and Organic Chemistry

Skip 491-513. Read 514-517

Heisenberg Uncertainty Principle

$$\Delta p \Delta x \geq \frac{1}{2} \left(\frac{h}{2\pi} \right) = \frac{1}{2} \hbar$$

WAVE { mvr ↓ relates to λ = h/mv } PARTICLE
 ↓
 position

CANNOT KNOW BOTH TO HIGH ACCURACY